An Analysis of Bitcoin with a Consumption and Savings Constraint

Traditionally, studies that replicate the equity premium puzzle with a Lucas Asset Pricing Model examine the excess returns of a risky security or index relative to those of risk free assets or treasury bonds. Until 2016, cryptocurrencies were largely unacknowledged by academics. Although the volatile behavior of cryptocurrency is now at the forefront of many financial economic works, the risk premia necessary to hold cryptocurrencies are scantly studied.This empirical work seeks to analyze the shock process of Bitcoin as wellas the shock process of relatively risk free U.S. Treasury Bills (i.e. to answer of a relatively risk free U.S. Treasury Bill?). Furthermore, this study seeks to examine the risk aversion parameter necessary to generate the level of equity return observed in the historical price data of Bitcoin and U.S. Treasury Bills (i.e. to generate the level of equity return observed in historical price data of Bitcoin and U.S. Treasury Bills?). B26 (Financial Economics), G14 (Information and Market Efficiency, Event Studies, and Insider Trading), L63 (Microelectronics, Computers, and Communications Equipment) Equity Premium; Technology; Cryptocurrency

There are two financial assets in which the representative agent can invest: a risk free Treasury Bill, , and cryptocurrency, . By borrowing or saving with the asset , the agent subsequently earns the risk free rate or return, . We suppose that the borrowing rate exceed the savings rate so that , and we let debt be non-defaultable with a borrowing limit .

Alternatively, the returns of cryptocurrency, , are calculated at time by with equal to the price of the Bitcoin price on day . Bitcoin earns a stochastic return during period where is assumed to be the innovation to excess returns distributed as . The stochastic return of Bitcoin follows a Markov Chain formally described as . The probability of landing in state is defined as Furthermore, the persistence of aggregate shock, , follows where the distribution of is defined as .

Given financial investments and , we compute financial wealth during period as . The representative agent must choose to save with risk free Treasury Bonds or to invest in Bitcoin. Provided that the representative agent has a utility function following with consumption, , and a risk aversion parameter of , a partial equilibrium in the infinite horizon model is met when the following value function in time is maximized. To solve for a partial equilibrium, we maximize the value function during time by choosing how much to invest in Bitcoin and Treasury Bills during period .

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